Graph Algorithms in a Guaranteed-Deterministic Language

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Abstract
Deterministic implementations of graph algorithms have recently been shown to be reasonably performant. In this paper we explore a follow-on question: can deterministic graph algorithms be expressed in guaranteed-deterministic parallel languages, which are necessarily restrictive in what concurrency idioms they employ? To find out, we implement several graph algorithms using the LVish library for Haskell, which provides an interface for guaranteed-deterministic parallel programming—essentially, a guaranteed-deterministic sublanguage embedded in Haskell. Doing so reveals strengths as well as limitations of the LVish approach. We surmount these limitations by (1) implementing a functional version of the deterministic reservations mechanism, and (2) adding a new mechanism to LVish called BulkRetry. We present results from an early-stage prototype.

1. Introduction
Graph algorithms, which analyze collections of nodes connected by edges, are important to many areas of computing. Indeed, their importance is increasing, in part driven by the availability of large graph data sets found in social networks and elsewhere. Parallelizing graph algorithms has been a priority [6,8,9] but is complicated by the fact that graph algorithms—such as breadth-first search (BFS), maximal independent set (MIS), or minimum spanning forest (MSF)—are irregular parallel algorithms, in which the amount of potential parallelism depends on the input graph.

Nevertheless, Blelloch et al., in a 2012 paper [2], demonstrate reasonably good parallel performance on a selection of graph algorithms in spite of those algorithms being internally deterministic. This determinism property has a number of benefits, including that multiple machines can execute the same algorithm with identical outcomes, unlocking possibilities for redundancy, failure recovery, or optimizations that trade re-execution against storage or network communication. Moreover, as has been widely recognized [7,13,14], deterministic systems are easier to debug during development.

Yet while the value of deterministic algorithms is widely recognized, how does one arrive at an implementation of a deterministic algorithm? The answer is usually "by writing code in a general-purpose, nondeterministic language"—that is, very carefully. Still, languages and libraries can make it easier or more difficult for developers to reach their determinism goal. For example, Blelloch et al. provide a toolbox of parallel collection operations such as scan, reduce, and filter. Using these operations, it becomes easier to write deterministic code—at least, easier than when using lower-level primitives like threads and locks directly.

In this paper we explore a more extreme proposition: implementing graph algorithms in a guaranteed-deterministic language. Rather than merely encouraging deterministic code, such a language makes it impossible to write nondeterministic code. Code written in such a language may be functionally incorrect, but the language implementation—the compiler and language runtime—guarantees that programs written in it cannot violate the determinism of the system.

By contrast, when using Blelloch et al.’s primitives, the programmer must still be trusted to follow a number of rules to ensure determinism. For example, certain operations, such as Blelloch et al.’s `find` and `link` operations on disjoint set data types, are allowed to run in parallel with one another, while others are not—and a mistake or oversight in following the protocol can result in nondeterminism of the entire application. Although programs written against such an unsafe API might be deterministic, they do not enjoy a language-level determinism guarantee.

One potential criticism of the approach of guaranteeing determinism at the language level is that when considering a complete software system consisting of compiler, runtime, libraries, and application code, there will always be a mix of code that is written in the guaranteed-deterministic language and code that is not. In fact, this is true not only with respect to determinism guarantees, but any language-level guarantee such as type safety and memory safety.

Still, there is a qualitative difference between unsafe programming environments, in which every new project involves new code that does not enjoy a language-level guarantee, and language-based approaches in which the amount of code without such a guarantee should be small and constant.

With the goal of minimizing the code without a language-level determinism guarantee, our approach is to begin with a deterministic host language, Haskell[^1], and combine it with a parallel programming library called LVish[^1]. LVish sanctions certain side effects on shared, mutable data structures as safe to use within otherwise functional applications. In this paper, we study how well-suited the LVish abstractions are to implementing graph algorithms, and describe extensions (Section 6) to the library that make it a better tool for efficiently graph algorithm implementations. We make the following contributions:

- We examine the parallel programming idioms used to `unsafely` implement three graph algorithms (BFS, MIS, MSF), comparing them to the simpler (blocking, dataflow) operations provided by LVish.
- We measure the performance of existing LVish primitives applied to graph algorithms, finding them wanting.
- We adapt the deterministic reservations mechanism to a functional, and guaranteed-deterministic setting.

[^1]: There are some caveats to our claim that Haskell is deterministic: programs that throw exceptions may not uniquely constrain which exception they throw; instead, it can be compiler-dependent. Also, while determinism holds for pure computations, it is possible to access a full imperative environment, in which every new project involves new code that does not enjoy a language-level guarantee, and language-based approaches in which the amount of code without such a guarantee should be small and constant.

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• We propose an extension to LVish, the BulkRetry primitive, to execute graph algorithms more efficiently while retaining the semantics of the simplest versions of the algorithms.

2. Background: LVars and LVish

Broadly speaking, deterministic languages use one or more of the following strategies to ensure determinism:

1. Restrict communication between parallel code regions (e.g., functional and dataflow paradigms).
2. Enforce permissions on who has access to shared data at each point in the program (e.g., Deterministic Parallel Java [3]).
3. Restrict writes to shared data to operations that commute.
4. Ensure threads proceed in lock-step (PRAM).

The LVish library supports a combination of options 1-3. It includes a basic mechanism for dynamic creation of parallel tasks: i.e., fork (t x) will enqueue the computation t x for execution on some processor. All communication between tasks happens through LVars, concurrent data structures whose states can be viewed as elements of a join-semilattice, and where the state of each LVVar may only grow monotonically with respect to that lattice. The simplest LVars are dataflow variables, called IVars [1], which may be either full or empty, and support a blocking operation. For example, with IVars, it is straightforward to replace fork—which does not return any values—with a notion of futures:

```haskell
import Data.LVar.IVar as IV

-- Define spawn-a-future in terms of IVars:
spawn comp =
  do vr ← IV.new
     -- Do the work in the child thread:
     fork (do res ← comp
              IV.put vr res)
     -- Return an IVar that serves as the future:
     return vr
```

More complicated LVars include concurrent data structures for sets, bags, finite maps, vectors, and so on, typically implemented using lock-free atomic memory operations. The existing LVish library includes a collection of such structures.

The determinism of LVish rests on the fact that operations on LVars commute. Modifications information, never subtract it, and observations of the state of LVars, when they return, yield an answer that is invariant under subsequent growth of the LVar’s state. We elide detailed explanation of the programming model here, referring the reader instead to previous work [10, 11]. However, one more programming primitive is necessary for our purposes.

`Handlers` Handlers in LVish are callbacks spawned every time an LVar changes. Though spawned on demand, they are equivalent to an infinite number of forked computations blocked and waiting on distinct gets. For example, we can easily write an LVish program to discover a connected component in a graph by creating an LVar to represent the set of seen nodes, by adding the starting vertex to that set, and using a handler to react to all new additions to the set by adding their neighbors:

```haskell
connected :: Graph → NodeID → Par (ISet NodeID)
connected g startV = do
  seen ← newEmptySet
  addHandler seen
  (λ nd → parMapM (putInSet seen) (nbs g nd))
putInSet seen startV
  return seen
```

The callback (the λ expression) is invoked only when the contents of the seen LVVar change. Repeated insertions of the same NodeID into the set will not cause redundant handler invocations. The Par return type of the connected function is a monadic type that indicates that the computation performs parallelism side effects. Yet, unlike the IO monad, the Par monad (12) can be used within purely functional code by using runPar, which has type Par a → a. This is possible because Par computations are deterministic.

3. Deterministic Graph Algorithms

We focus on three fundamental graph problems in this paper:

• **Breadth-first search**: Given a graph \( G = (V, E) \) and a source vertex \( s \in V \), return a BFS tree with root \( s \) and nodes from \( V \).

• **Maximal independent set**: Given a graph \( G = (V, E) \), return a set \( S \subseteq V \) such that no two vertices in \( S \) are neighbors, and all vertices not in \( S \) have at least one neighbor in \( S \).

• **Spanning forest**: Given an undirected graph \( G = (V, E) \), return a collection \( F \subseteq E \) such that \( \forall i, \exists T_i \in F \) where \( T_i \) is a spanning tree for \( C_i \), a connected component of \( G \).

**Tie-breaking** All three of these algorithms may have multiple valid answers for a given input graph, and thus nondeterministic answers are often acceptable. To achieve a deterministic result, tie-breaking between valid answers is required—for instance, if there are two valid BFS tree topologies, we must select one consistently. This is often accomplished by allowing vertex IDs to serve as priorities. For example, when selecting which of two valid parents to choose in a BFS tree, we can guarantee that we select the higher-priority parent, at the expense of some extra work.

Without specifying a particular implementation strategy, we may still observe that certain primitives are required for parallel implementations of these algorithms:

• **Reduction variables or prioritized writes**: To record the highest-priority parent of a particular vertex, or to maintain an intermediate state of a growing spanning forest, we need reduction variables that support commutative operations.

• **Parallel schedules corresponding to data-dependent priorities**: The parallelism in these algorithms mirrors the structure of the graphs; we need a way to process vertices in parallel and yet ensure that higher-priority vertices or edges take their turn first. We will see that this can be accomplished either with blocking dataflow-style communication, or with other mechanisms that achieve the same effect (Section 4.3).

In the next section, we present simple and safe formulations of graph algorithms using LVars to provide the above capabilities. In Section 5, we review how these algorithms have been implemented efficiently and deterministically in previous work (2), unsafe APIs and primitives. Finally, in Section 6, we will attempt to reconcile the two, improving the efficiency of the LVar-based implementations.

4. Graph Algorithms in LVish

In this Section we show how to apply existing LVish primitives to implement the algorithms BFS and MIS. Then, we demonstrate how the deterministic reservation concept can be implemented using existing LVish primitives, thereby gaining guaranteed determinism and losing space efficiency.

4.1 Breadth-first search trees

We already showed a simple example of a connected component computation, which performs an asynchronous, parallel depth-first traversal of a graph. Here we show a modification of the algorithm

to return a full BFS tree topology, as in [2], rather than merely returning the set of node IDs in the connected component.

As mentioned in Section 3, we need to use a reduction variable to keep track of only the minimum or maximum NodeID that could be a parent for a given node; that is, a MinVar instead of an IVar (both being instances of LVars).

```haskell
import Data.LVar.MinVar

type NodeID = Int

bfsTree :: Graph → NodeID → Par (Vector MinVar)
bfsTree gr start = do
  -- Decompose into vertex and edge vectors:
  let (Graph verts edges) = gr
      -- A new array with a MinVar for each vertex:
      parents ← Vector.generateM (length verts)
      (λix → newMinVar maxInt)
  seen ← newEmptySet
  handler nd = mapM (eachNbr nd) (nbs gr nd)
  eachNbr nd nbr = do putInSet seen nbr
    -- Write ‘nd’ to the MinVar:
    putMin parents nbr nd
  addHandler seen handler
  -- Register callback.
  putInSet seen start
  -- Kick things off.
  return parents
```

Each MinVar in the parents vector begins initialized to maxInt and will be overwritten with a smaller number if it is part of the connected component. As before, the handler attached to seen drives the computation. Note, however, that LVish programs are generally asynchronous, and non-blocking where possible. For example, the bfsTree function above returns immediately, not waiting for the cascade of handler invocations to complete. Rather, a synchronization operation is required to wait on spawned tasks to complete and freeze the final value of the parents array above (see [11]).

4.2 Maximal independent set

In LVish, our implementation of the maximal independent set algorithm closely matches the greedy algorithm that is usually described as follows: iterate over the vertices of the graph and grow the independent set by adding a vertex to it only if none of its (higher-priority) neighbors have been already included. Because processing a vertex depends only on higher-priority neighbors, cycles in the graph do not cause cycles in loop iteration dependencies.

Here is the LVish code, which uses an IStructure datatype equivalent to an array of IVars:

```haskell
data Flag = Chosen | NbrChosen

mis :: Graph → Par (IStructure Flag)
mis gr = do
  let (Graph verts edges) = gr
      flagsArr ← newIStructure (length verts)
  parFor (0, length verts) (λix → do
    let checkNbr acc nbr = do nbrFlag ← get flagsArr nbr
        case nbrFlag of
          Chosen → do put flagsArr ix NbrChosen
                    return True
        _ → return acc
    -- Only if none of the nbrs are chosen can we:
    unless nbr_chosen ← foldM checkNbr False (nbs gr ix)
    return flagsArr
  )
```

Each vertex is assigned one of three flags representing the status of the vertex with respect to the computed independent set: Chosen, NbrChosen, or undecided, with undecided represented not explicitly, but by an empty slot in the IStructure. The output of the LVish program is an IStructure Flag, i.e., an array of IVars, each containing a flag and corresponding to a single vertex. IVars are the very simplest form of LVars that are either empty or full, and contain at most a single value. In LVish, IVars allow for multiple puts of the same value, and also provide a get operation that blocks when the IVar is empty.

4.3 Minimum spanning forest

Minimum spanning forest provides an interesting example where LVish is not a good fit out of the box. This is in contrast with BFS and MIS, where blocking gets provide exactly the required synchronization, and monotonic updates are the only concurrent writes. To implement MSF, we needed to add a new library function based on a technique introduced in [2]. We describe that mechanism here before proceeding.

**Deterministic Reservations** are a method of parallelizing iterative greedy algorithms introduced by Blelloch et al.. A C++/Cilk implementation is available as part of the Problem-Based Benchmark Suite (PBBS). The approach focuses on the deterministic parallel processing of loops with loop-carried dependencies. The idea is to allow the user to break the iteration space into rounds, where each round selects a deterministic subsets of available iterates which have no conflicting reads or writes. No attempt is made to automatically detect conflicts, rather they are declared and checked by the user.

The main algorithm takes in a sequence of iterates and consists of a series of rounds. In each round, a predetermined prefix of the iterates is processed in two phases, each of which are parallel loops over the prefix. The first phase runs the reserve routine of each iterate in the prefix, which resolves data conflicts by reserving the access to shared data through (deterministic) priorities. The second phase computes the commit component of each iterate, processing those iterates for which the reservations succeeded. The failed iterates, along with new iterates, are part of the next prefix for the subsequent round, and the algorithm thus proceeds until all iterates have been exhausted.

The formulation of deterministic reservations in LVish is somewhat different, because arbitrary side effects are not permitted in parallel. Instead, it takes the form of a supercombinator that takes five arguments:

```haskell
forSpeculative (0,n) state0 reserve commit update
```

The full type of the function is:

```haskell
forSpeculative :: (Ord b) ⇒ (Int,Int) → Either b → Either b
```

Both the MIS and BFS implementations in LVish use fully asynchronous, data-driven scheduling. This is in contrast to the PBBS implementations, where MIS and BFS use deterministic reservations and are therefore scheduled in synchronous rounds.
The main difference from the C++ version is that this version routes a state argument, \( st \), through each phase of each of the rounds, giving the user the chance to update the state once per round. The three phases (reserve, commit, update) are composed sequentially, with barrier synchronizations between; update is not a loop, but a single callback after the commit phase but before the next round. In the reserve phase, the user’s function optionally returns a value of type \( b \). If it does, that signals that the iteration should attempt to commit this round. The \( b \) returned by the reserve call is then passed to the commit call for the same iteration. The iteration may still fail in the commit phase, however, which is why commit returns a \( Bool \), with true indicating a fully successful commit.

Regular LVish side effects (monotonic updates) are permissible in any of the reserve, commit, and update functions. Indeed, recall that anything permitted by the type system must at least retain determinism. There are no informal contracts that must be fulfilled. However, since only monotonic updates are allowed as side effects, if we wish to update a data structure multiple times we will have to do so out-of-place (in a functional style). Frequently, we will allocate new LVars in the update phase, and then mutate them in the reserve phase and read them in the commit phase (or vice versa). Unfortunately, these use-once LVars are a source of additional memory allocation and inefficiency relative to in-place versions.

**Parallelizing MSF** Minimum spanning forest can be implemented by first sorting edges by weight, and then sequentially processing edges, greedily adding them to the spanning forest if they are not already redundant. To check redundancy, a disjoint sets data structure is maintained, which tracks to which set each vertex belongs at each point in the algorithm. The PBBS deterministic parallel implementation is simply a speculative version of the sequential loop. The writes performed by each iterate are to link two disjoint sets together by including a new edge in the spanning forest. These writes must not conflict, and so priority based “locking” must be used during the reserve phase to ensure that non-conflicting iterations are executed in parallel.

To code the algorithm in LVish, we first define a new datatype to hold the state between phases at \( st \):

```haskell
data MsfState = MsfState { lastSets :: Vector NodeID, thisSets :: IStructure NodeID, reserves :: Vector MinVar }
```

Here, we use an array of NodeID to represent the disjoint sets. That is, we use NodeID as the set identifiers, and the Vector NodeID says, for each index \( i \), which set identifier the \( i \)th vertex falls under. thisSets and lastSets are two copies of the same thing. Because our version of this algorithm is out-of-place, we separately keep the disjoint sets data structure from the last round (lastSets, read only), and the one that we populate this round (thisSets, write only).

Note that the type of these two arrays is different, Vector vs. IStructure, because the former is a regular Haskell array, and the latter is an LVar. The IStructure is converted into a vector at the end of the round by freezing it \( [\text{Vector}] \). This prevents further modifications, but snapshots the LVar so that regular Haskell code can have full access to consume the contents.

We will not go over the whole code for MSF, but will look at the important pieces. The reserve function passed to forSpeculative is given by:

```haskell
-- Reserve an iteration which corresponds to an edgeid: reserve eid MsfState{lastSets,reserves} = do

let (a,b) = edges![eid]
    (u,v) = if a>b then (b,a) else (a,b)
    set = lastSets!u

if u == v
    then return Nothing
else do -- Attempt reservation:
    putMin (reserves!set) eid
    return (Just ())[11]
```

Here we see the LVar MinVar again. It is used to implement the priority write. In this case, the minimum eid written to a set’s MinVar during the reserve phase is the winner for that round. The final MinVar value is read out in the commit phase to check who won:

```haskell
commit finalOutput eid MsfState(lastSets,thisSets,reserves) () = do
    let (u,v) = edges![eid]
        (uset,vset) = (lastSets!u, lastSets!v)
    winner ← freezeMinVar (reserves!uset)
    if (winner == eid) then (do
        -- Mark this edge as included in the final output:
        put finalOutput eid ()
        let newSetId = min uset vset
            -- Link disjoint sets together in the next round:
            put thisSets uset newSetId
            put thisSets vset newSetId
        return True)
    else return False
```

### Determinism Guarantee

For speculative, like all LVar library functions, guarantees determinism irrespective of the reserve and commit functions the user writes. In part, this is enforced by runtime checking of the consistency of writes to LVars. Problems that would otherwise cause nondeterminism are explicitly caught (deterministically) and raised as exceptions: for example the “multiple-put on IStructure” exception.

Finally, there are some interesting possibilities enabled by the above formulation of deterministic reservations. Because arbitrary Par effects can occur in any iteration of the reserve or commit functions, this means that a reserve can do blocking reads on far-away data, and that, like most LVish functions, the speculative for loop can consume partially populated data structures incrementally.

### 5. Unsafe Deterministic Implementations

Having seen deterministic-safe formulations of the algorithms BFS, MIS, and MSF in LVish, we now review where the liabilities lie when implementing the very same algorithms in a general purpose (non-deterministic) parallel language, as in the PBBS C++ reference implementations.

The deterministic algorithms in PBBS rely on shared state that is accessed concurrently on multiple processors: this is the only form of communication between tasks. And yet it must be used carefully: operations on shared state must be commutative and linearizable, further, for deterministic reservations, all potential loop dependencies must be enumerated explicitly by the programmer without missing any. Finally, APIs (such as disjoint sets’), which provide methods that are threadsafe individually but not mutually, require the user to think carefully about phases and barrier synchronization to maintain determinism.

The simplest example is in the memory cell data type supporting a priority read and write, which can be used for selecting among parallel choices. It has the property that while two priority writes commute, a priority read and write do not commute. The programmer thus has to ensure that operations containing priority reads are not called in parallel with those containing priority writes.

A further example can be seen in the priority reserve datatype that supports the operations of reserve, check, and checkR...
(check-and-release), all taking a priority $p$ as input. This structure comes with two subtleties – reserves and checks (of either form) do not commute, and two checks commute only when called with distinct priorities. For disjoint sets, the operations of $\text{find}$, which finds the set associated with its argument, and $\text{link}$, which performs a logical union of sets, are not provided to be linearizable. In all these cases, care must be taken to write programs with parallel blocks that contain only those particular forms of abstractions that commute and are linearizable.

6. **One solution: BulkRetryT**

So far, we have seen asynchronous LVish formulations of three graph algorithms, and we have reviewed bulk-synchronous C++ implementations from previous work [2]. The latter are fast, and written as unsafe code that must be relied upon. The former use determinism-safe primitives, and unfortunately are slow. In fact, their performance problem is unlikely to be solved by further tuning of the code and ironing out of Haskell/C++ performance differences. The problem is that each of the LVish algorithms (BFS, MIS, MSF) schedules $O(|V|)$ or $O(|E|)$ parallel tasks; further, these tasks may block if its dependencies are not met, which in turn means storing a continuation and rescheduling when its dependency is fulfilled. Each of these steps incurs overhead interacting with the parallel scheduler that is paid on a per-vertex/per-edge basis and cannot be amortized.

PBBS, on the other hand, is able to reduce overhead with the following techniques:

- Using parallel loops that *never* require per-iteration interaction with the parallel scheduler. Even though Cilk’s $\text{par}$ is comparatively efficient, per-vertex/edge is too fine-grained.

- Never storing state for loop iterates that fail to run, beyond the indices of the iterates themselves. That is, PBBS uses a retry strategy rather than a blocking one.

Can we achieve the same benefits while keeping a guaranteed-deterministic programming interface in LVish? Fortunately, yes, but slightly different techniques are required to be robust against *arbitrary inter-iteration dependencies.*

[Not] Assuming sequential-loops The deterministic reservation mechanism used in PBBS executes a *speculative* parallel evaluation of semantically-sequential loops. That is, iteration $i + k$ may depend on $i$ (forward dependencies) but not the other way around (reverse dependencies). Unfortunately, while this assumption is reasonable for many algorithms, it cannot be enforced by the compiler when loop iterations run arbitrary C++ or Haskell code.

PBBS’s *speculative for* can run away on reverse dependencies because it processes a constant-sized prefix of loop iterations in each round. Thus, if all the iterations in a given round fail, then the algorithm tries exactly the same iterations again the next round and does not make progress. This problem could be fixed by expanding the prefix each round so that it would eventually encompass all iterations. In the worst case, the very last iteration is the only one that is enabled to run. Unfortunately, this approach can explode the number of times the reserve phase of the iterates are run to $O(N^2)$ for $N$ loop iterations.

The problem is even worse for LVish loops with potentially blocking iterates: running two iterates sequentially for performance reasons results in deadlock if they have a reverse dependency. This would seem to require that each iterate be a parallel task, which we know is inefficient. A better solution to amortizing scheduler overhead while avoiding deadlock is to switch to a *retry* strategy.

Abort/retry rather than blocking For any parallel language that is both deterministic and in which all tasks are idempotent (like LVish), it is possible to retry tasks rather than blocking them. That is, if a task $T$ encounters an unmet dependency, rather than storing its continuation at that point, it can simply be rescheduled for execution later (ideally after the dependency has been updated).

This abort/retry scheduling approach is already used by some systems, including Intel’s Concurrent Collections (CnC) [4]. Abort/retry becomes especially beneficial when considering parallel loops rather than individual tasks. Registering a task with its dependencies to be re-executed when the dependencies change still requires significant per-task bookkeeping, which we would not want to pay for each iteration of a parallel loop. Rather, when executing a parallel loop we can try many iterations in bulk, and then retry them in bulk. Indeed, this is exactly the strategy used by PBBS’s *speculative for*.

**BulkRetry in LVish** To include a retry-based parallel for-loop in LVish, we need to be able to optionally intercept blocking get operations and instead register the failed iteration numbers in a data structure. Fortunately, the semantics of LVish get operations assure that we will not need to worry about idempotence for the re-executed portion of the task. We use a tweaked version of the Par monad *(i.e. we layer on a “monad transformer”)*. This tweaked Par monad keeps in thread-local state an arbiter object representing the current parallel loop; when blocking operations are encountered it checks whether the computation is currently in a loop:

- If in loop: register the failed iteration with the loop arbiter. Escape from the current loop iteration.
- Otherwise: block normally.

One advantage of the BulkRetry mechanism is that only minor modifications are required to reuse the BFS and MIS implementations from Section 4. First, the type must be changed from a vanilla Par to a BulkRetryT Par. Second, the parallel loop, for example in MIS, must be replaced with its bulk-retry counterpart.

The disadvantage of BulkRetry is the same as for speculative in PBBS: the schedule is constrained by synchronous rounds. That is, rather than retrying an aborted task as soon as its dependencies are updated, it must wait until the next round before retrying. However, this reduction in parallelism should not be a problem, as the prefix sizes are chosen to ensure abundant parallelism within each round.

7. **Evaluation, Future Work, and Conclusion**

Our prototype is complete and functional, but requires much tuning work to improve the constant factors in its performance, and to improve scaling of the runtime system. For example, sequential performance of MIS is 19.1× slower than the C++ code delivered with PBBS. However, our main hypothesis, that BulkRetry will improve overheads and scaling, is borne out in Table 1.

General Haskell/C++ differences account for much of our current performance problems, although careful tuning of the Haskell code should be able to narrow this gap to under 3×. Other overheads will be more difficult to address: namely, Haskell code tends to be allocation intensive, and its garbage collection (when using the GHC compiler) is parallel but not concurrent. Our graph benchmarks spend over 50% of their time in GC with four or more threads. Nevertheless, GHC is the only mature compiler that provides the determinism guarantee we require, and thus we will continue to work on these issues.

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4 Although language-level enforcement of idempotence is not possible in the case of CnC, whose flagship implementations are in C++ and Java.

5 On the random local graph topology, with 10M vertices.
### Table 1. Running times (in seconds) for three graph topologies for the vanilla LVish and BulkRetry MIS implementations. Run on a 4-core Intel i7-3770 CPU at 3.40 Ghz.

<table>
<thead>
<tr>
<th>MIS</th>
<th>random local</th>
<th>rMat</th>
<th>3D grid</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>( n = 10^7 )</td>
<td>( n = 10^7 )</td>
<td>( n = 10^7 )</td>
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<tr>
<td>( m = 5 \times 10^7 )</td>
<td>( m = 5 \times 10^7 )</td>
<td>( m = 5 \times 10^7 )</td>
<td></td>
</tr>
<tr>
<td>misI3</td>
<td>24.363</td>
<td>38.740</td>
<td>21.436</td>
</tr>
<tr>
<td>misBR</td>
<td>7.419</td>
<td>10.090</td>
<td>6.700</td>
</tr>
</tbody>
</table>

**Pipelining latency benefits** In spite of their poor throughput on their own, the Haskell MIS and BFS implementations are fully asynchronous, which allows them to work well when they are one kernel among many in a larger application. For example, if a downstream phase of processing processes a connected component discovered by a call to BFS, then it can begin executing as soon as a single vertex is discovered, not waiting for the BFS to complete. In a worst-case scenario of a graph containing a linear chain (of, say, 10M vertices), this makes the difference between downstream computations starting after 9 seconds (C++/PBBS) vs. under a millisecond (LVish).

**More data structures** The graph benchmarks in this paper are data-structure intensive workloads. Probably the most significant region for improvement is not in the GHC compiler itself, but in the data structure libraries, both included with LVish and otherwise. For example, we use the existing ‘Data.LVar.SLSet’ data structure (based on a concurrent skip-list) for storing failed iterates. It supports balanced parallel iteration after freezing, but is still a high-bookkeeping, GC-unfriendly data structure. A hierarchical bit-vector may serve better for the purpose of storing failed iterates. Exploring this and other data-structures, in addition to tuning the LVish scheduler, will be primary focuses of our future work.

**References**


